

A Comparative Study of the Chemisorption of Ethene on three Metal Surfaces: Ni(111), Pd(111) and Pt(111)

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The chemisorption of ethene on three metal surfaces, Ni(111), Pd(111) and Pt(111), has been studied by an approximate molecular orbital method: extended Hückel calculations within a tight-binding formalism. The overlap population between individual fragment molecular orbitals (FMO) of the adsorbate and each atomic orbital (AO) or atom of the surface can be partitioned accurately. The relative importance of each FMO to the ethene-metal bonding can then be assessed. Moreover, interaction diagrams can be constructed to describe the adsorbate-surface bonding. The preferred adsorption sites determined by our calculations are supported by the vibrational data obtained by electron energy loss scattering. The activation energy for the transformation of π -bonded ethene to di- σ -bonded adsorbate on Pt(111) has been estimated.

Heterogeneous catalysis on metal surfaces implies enhanced reactivity. Facilitation of a reaction may occur in any of the many steps of a surface mechanism, *e.g.* chemisorption, reaction, migration on the surface, further reaction, desorption. If we are to understand these reactions, we have to understand them in detail for one metal, and, most importantly, how they vary as we pass from one metal to another.

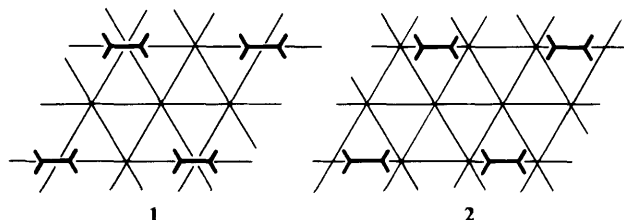
The common crystal forms of the group 10 elements Ni, Pd and Pt are face-centred cubic. The hexagonal (111) face is a close-packed plane, likely to be minimally reconstructed. For a given adsorbate, we might expect a smooth, gradual change in adsorbate-surface interaction as we go from Ni(111) \rightarrow Pd(111) \rightarrow Pt(111). Consider now specifically ethene. Electron energy loss scattering (EELS) showed that ethene is more strongly bound and more distorted on Ni(111) and Pt(111) than on Pd(111).¹ Comparison of the vibrational spectra also suggested a different adsorption site on Pd(111).² This is inconsistent with the simple idea of a gradual change and poses a puzzle.

In this paper, we investigate the chemisorption of ethene on the above-mentioned three metal surfaces. The tight-binding extended Hückel method is employed to trace the orbital interactions.³ As a compromise between accuracy and economy, three-layer slabs serve as models for the metal surfaces. The adsorbate molecules are put on one side of the two-dimensional metal slabs only. This covered layer will be referred to hereafter as the surface layer.

Let us first review the experimental data in some detail, for these have been the subject of some controversy. Ethene adsorbs initially in a disordered way on Pt(111). After exposure to the electron beam (and probably some decomposition) a (2×2) low energy electron diffraction (LEED) pattern can be observed, indicating a possible coverage, θ , of 0.25.⁴ This value of θ was supported by thermal desorption spectroscopy⁵ and radiotracer data,⁶ but disagreed with results from X-ray photoelectron spectroscopy⁷ and elastic recoil detection.⁸ The latter two methods favoured $\theta = 0.5$. Our calculations will show that for one-half coverage there are extremely large adsorbate-adsorbate repulsions, unless the ethene molecules are tilted with respect to the surface. This upright position has been detected only on the Pt(111) surface near 300 K, at which temperature decomposition occurred.⁹ We wish to concentrate here on low-temperature adsorption where the C-C bond is parallel to the surface.¹⁰ So one-quarter coverage seems to be more reasonable. A (2×2) LEED pattern has been obtained for ethene on Ni(111) as well.¹¹ The Pt-Pt bond length (2.77 Å)

is only slightly longer than that of Pd-Pd (2.75 Å). We thus assume the same coverage, $\theta = 1/4$, for all three metal surfaces.

Although the exact geometry and location of the chemisorbed ethene are unknown, some useful information is available. EELS performed near 100 K pointed to a 2-fold bridge site (di- σ -bonded ethene), **1**, for Ni(111) and Pt(111) but an on-top site (π -bonded ethene), **2**, for Pd(111).^{2,12-15} The assignment of adsorption site for Ni(111) was supported by near-edge extended X-ray absorption fine structure (NEXAFS).¹⁶ This technique, however, favoured a π -bonded adsorbate on Pt(111).⁹ Adding to this controversy are the recent results of ultraviolet photoelectron spectroscopy (UPS) which suggested the existence of a π -bonded species at temperatures lower than 52 K on Pt(111). At temperatures higher than 52 K, the adsorbate transforms into di- σ -bonded ethene.¹⁷ Finally, it is interesting to note that the di- σ -bonded ethene was proposed to be the intermediate for catalytic exchange between ethane and deuterium (the $\alpha\beta$ process) over an evaporated film of Ni, Pd and Pt. More recently, the involvement of a π -bonded alkene has been proposed.^{18,19} By adjusting the geometry of the ethene to fit the photoemission results, Demuth suggested C-C bond lengths in ethene of 1.39, 1.44 and 1.49 Å on Ni(111), Pd(111) and Pt(111), respectively²⁰ (compared to 1.37 Å in Zeise's salt) and some bending of hydrogen away from the surfaces. The C-C bond lengths on Pd(111) and Pt(111) are in excellent agreement with the NEXAFS data (1.43 and 1.49 ± 0.03 Å, respectively).^{10,21} Room-temperature adsorption of ethene on Ni(111) produced a C_2 surface species with a C-C bond of *ca.* 1.45 Å.¹⁶ Recent studies on Cu(100) led to a C-C bond lengthening of *ca.* 0.13 Å.^{22,23}



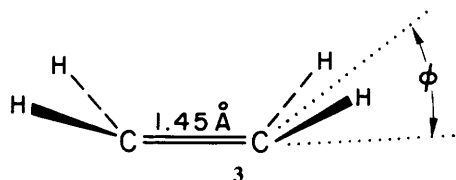
To simplify the problem within our computational ability, all the C-C bonds, the C-H bonds and the HCH angles of ethene on the three surfaces studied are set to 1.45 Å, 1.10 Å and 120°, respectively. The Ni-Ni, Pd-Pd and Pt-Pt bond lengths are kept fixed at 2.49, 2.75 and 2.77 Å. No surface reconstruction or relaxation is presumed. From the

Table 1 Optimized HCH bending angles (ϕ , see 3) of ethene with metal surfaces

| metal surface | bending angle/ $^{\circ}$ | |
|---------------|---------------------------|-------------|
| | 2-fold site | on-top site |
| Ni(111) | 40 | 30 |
| Pd(111) | 25 | 15 |
| Pt(111) | 39 | 25 |

known structures of organometallic compounds and the theoretical work of Anderson,²⁴⁻²⁷ we assume a metal-carbon bond length of 2.02 Å for ethene on Ni(111) and 2.10 Å on Pd(111) and Pt(111).

The degree of bending of the hydrogens should be different for each metal surface. The bending angles of the HCH planes with respect to the metal surfaces (ϕ , as defined in 3), were determined by minimizing the total energy. Table 1 displays the optimized bending angles. Despite our drastic approximations, for a given adsorption site ethene seems to prefer a less distorted geometry on Pd(111), in agreement with the experimental result.



Before we proceed to a detailed analysis of the adsorbate-surface interaction, a few words are in order about the two important conceptual tools we use: the density of states (DOS) and its partitions, and the crystal orbital overlap population (COOP) curve. The DOS curve is a graph of the number of orbitals per unit volume per unit energy as abscissa, *vs.* energy as ordinate. DOS may be partitioned on an atom, atomic orbital or fragment molecular orbital basis. The COOP curve is a plot of the overlap population-weighted density of states *vs.* energy. Integration of the COOP curve up to the Fermi energy then gives the total overlap population.³ Further computational details can be conveniently found in the Appendix.

Comparison of the Adsorption of Ethene on Ni(111), Pd(111) and Pt(111)

One of the drawbacks of the non-self-consistent extended Hückel method is the exaggeration of electron transfer. The

valence-state ionization energies (H_{ii}) for the metals are thus refined by charge iteration of the three-layer slabs with ethene at the 2-fold site and the on-top site until self-consistency in the metal charge distribution is attained. In this way, the excessive electron flow is greatly reduced. Table 2 gives the H_{ii} s of the s, p and d orbitals of Ni, Pd and Pt so obtained. Among the three metals, the energy difference between the d orbitals and the s or p is greatest for palladium. As we shall see later, this leads to some interesting bonding features. Note that the two sets of charge self-consistent parameters are not that different.

It is instructive to compare our computed results with those obtained by other theoretical methods. Relativistic augmented-plane-wave calculations suggest that the palladium d band is lower than that of the platinum.²⁸ This computational technique also indicates that compared to palladium, the platinum sp bands move towards lower energies relative to the d band. There is thus stronger sp-d hybridization in the case of platinum.

Calculations have been performed with both sets of parameters (those derived from the on-top and 2-fold site iterations). Selected results for the '2-fold site parameters' are listed in Table 3 and those for the 'on-top site parameters' in Table 4. The binding energy is defined as the difference in energy between the adsorbate-surface composite system when the planar, undistorted ethene molecule is removed from the surface and when it is chemisorbed with the above specified geometry. A positive binding energy means an attractive interaction.

The energies in these calculations are computed as a simple one-electron sum of the energies of the occupied orbitals. Studies of many organic, and inorganic discrete molecules and extended systems have shown that the extended Hückel method is moderately reliable; it tends to give trends in bonding preferences and electron shifts approximately correctly, but the actual magnitudes may be far astray.^{29,30}

It seems that on Ni(111) and Pt(111) there is a slight preference for the 2-fold site over the on-top site. The reverse is true on Pd(111). Comparing the binding energy at the 2-fold

Table 2 Valence-state ionization energies (in eV) obtained by charge iteration with the ethene molecule at the 2-fold or on-top site

| metal surface | 2-fold site | | | on-top site | | |
|---------------|-------------|-------|--------|-------------|-------|--------|
| | s | p | d | s | p | d |
| Ni(111) | -7.92 | -4.18 | -11.51 | -7.79 | -4.08 | -11.30 |
| Pd(111) | -7.51 | -3.86 | -12.53 | -7.50 | -3.85 | -12.51 |
| Pt(111) | -8.82 | -5.28 | -12.15 | -8.75 | -5.23 | -12.04 |

Table 3 Binding energies and C—C overlap populations calculated with the 2-fold site parameters

| metal surface | 2-fold site | | on-top site | |
|---------------|-------------------|------------------------|-------------------|------------------------|
| | binding energy/eV | C—C overlap population | binding energy/eV | C—C overlap population |
| Ni(111) | +0.404 | 0.902 | -0.172 | 0.968 |
| Pd(111) | +0.229 | 1.040 | +0.313 | 1.066 |
| Pt(111) | +0.583 | 0.914 | +0.401 | 0.972 |

Table 4 Binding energies and C—C overlap populations calculated with the on-top site parameters

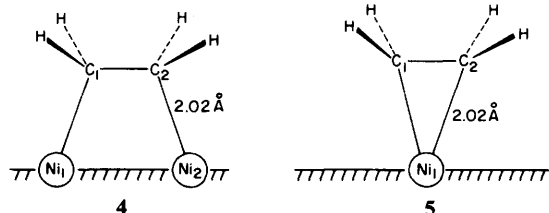
| metal surface | 2-fold site | | on-top site | |
|---------------|-------------------|------------------------|-------------------|------------------------|
| | binding energy/eV | C—C overlap population | binding energy/eV | C—C overlap population |
| Ni(111) | +0.476 | 0.894 | -0.147 | 0.962 |
| Pd(111) | +0.232 | 1.040 | +0.316 | 1.066 |
| Pt(111) | +0.614 | 0.910 | +0.446 | 0.971 |

site of Ni(111) and Pt(111) with that at the on-top site of Pd(111) suggests that chemisorption on the latter may be weaker. The adsorption of ethene on Pt(111) occurs even at 37 K.¹⁷ The activation energy for adsorption should be vanishingly small. The activation energy for desorption would then be a good upper bound for the binding energy. The activation energy for desorption of the di- σ -bonded and the π -bonded ethene on Pt(111) are determined experimentally to be 0.39–0.74 and 0.22–0.39 eV, respectively.^{31,32} The computed binding energies for ethene on Pt(111) are probably of the correct order of magnitude.

The C–C overlap population (OP) of ethene and ethane at their equilibrium geometries are 1.300 and 0.737, respectively. Hence the computed overlap populations point to a bond order of *ca.* 1.5. The C–C OP for the more stable adsorption site on Ni(111), Pt(111) and Pd(111) is calculated to be 0.902, 0.914 and 1.066, respectively (using the 2-fold site parameters). The C–C stretching frequencies for ethene on Ni(111), Pt(111) and Pd(111) appear to be 1045, 1110 and 1355 cm^{-1} , respectively,³³ the first two values being the mean values from the surface species derived from C_2H_4 and C_2D_4 , and the third from the C_2D_4 species alone because the C_2H_4 spectrum (like that of Zeise's salt and of ethene itself) is complicated by strong coupling between C–C stretching and CH_2 scissors modes.³⁴ An alternative assignment is 1200, 1230 and 1502 cm^{-1} .^{1,14} Values for Zeise's salt $[\text{KPtCl}_3(\text{CH}_2=\text{CH}_2)]$ and free ethene in the gas phase are 1515 and 1623 cm^{-1} , respectively.

The agreement between the computed results and experiment is reasonable and the trend is not very parameter-sensitive (compare Tables 3 and 4). Similar qualitative features are obtained with either set of parameters, except that the $H_{ii}s$ for the on-top site generally give a slightly higher binding energy. Hereafter our discussion will be based on the results derived from the 2-fold site parameters.

The numbering of atoms at the two adsorption sites of Ni(111) is depicted in 4 and 5. Since (2×2) unit cells have been chosen (see 1 and 2), there is always a mirror plane bisecting and perpendicular to the C–C bond. Hence, in every adsorption site there are two symmetry-equivalent C–Ni bonds: the $\text{Ni}_1\text{—C}_1$ and $\text{Ni}_2\text{—C}_2$ bonds at the 2-fold site, and the $\text{Ni}_1\text{—C}_1$ and $\text{Ni}_1\text{—C}_2$ bonds at the on-top site. To compare the bonding between 4 and 5, it is sufficient to single out one of the two C–Ni bonds. Hereafter, whenever we refer to the COOP curve or overlap population of a C–Ni bond, we imply the $\text{Ni}_1\text{—C}_1$ bond, be it at the on-top site or the 2-fold site (unless otherwise specified). For compactness, the 2-fold site and on-top site on Ni(111) are abbreviated as Ni(2-fold) and Ni(on-top), respectively. The same conventions apply to the other two surfaces.



From the experience of organometallic chemistry, and the supporting theoretical framework of perturbation theory, we know that the interactions between the central metal atom and its ligands occur mainly through the frontier orbitals. The frontier orbitals of bent ethene are, in order of increasing energy, σ_π , σ , π and π^* , 6, the first three of these being fully occupied in neutral ethene. (σ_π is C–H σ -bonding and C–C π -antibonding. This is the inspiration for our nomenclature.) We expect them to play an important role on the adsorbate-

surface interaction. As we shall see later, for the on-top site on Pd(111) and the 2-fold site on Ni(111) and Pt(111), these orbitals are responsible for 125, 99 and 98%, respectively, of the carbon–metal OP. (The contribution on Pd(111) is greater than 100% because all the other eight orbitals of ethene produce a net antibonding OP of -0.041 .) Thus, the following analysis will concentrate on these four frontier orbitals.

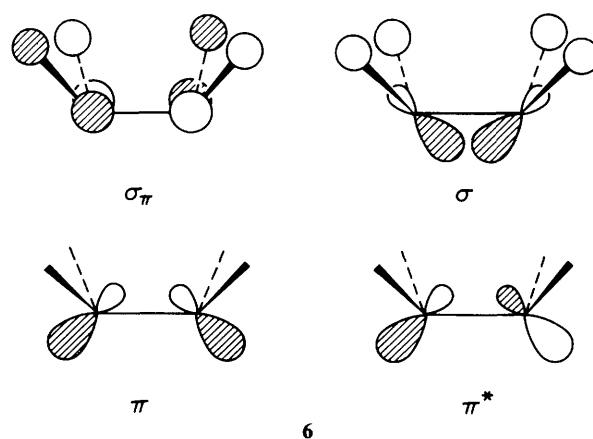


Fig. 1 is the analogue of an interaction diagram in molecular chemistry. In the left panel (a) is the total density of states (DOS) of a monolayer of ethene arranged in the same geometry as the adsorbed layer at the 2-fold site of Ni(111). The π and π^* band then correspond to the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) of a discrete molecule. There is extensive overlapping of the DOS of σ and σ_π near -15 eV.[†] Judging from the narrowness of the bands, the adsorbate–adsorbate interaction at one-quarter coverage is small. This is expected for the closest H···H contact between neighbouring ethene molecules at this coverage is 2.42 Å. Energetically, this steric interaction costs only *ca.* 0.049 eV.

The right panel (c) is the DOS of the bare Ni(111) surface. The position of the Fermi energy suggests that most of the d bands are filled. Indeed, for the surface atoms of bare Ni(111), Pd(111) and Pt(111), the computed electronic configurations are $d^{9.47} s^{0.40} p^{0.18}$, $d^{9.81} s^{0.10} p^{0.09}$ and $d^{9.36} s^{0.46} p^{0.23}$, respectively. The electron occupation of the valence s orbitals seems to be slightly lower, and that of the p orbitals slightly greater, than would have been anticipated. The width of the d bands is *ca.* 4 eV, while the dispersions of the s and p bands are much larger, reflecting the much more contracted nature of the d orbitals.

In the middle panel (b), we display the total density of states of ethene (shaded) after adsorption. In reality, the Fermi energy of the metal surfaces should not move after adsorption. It does so in our calculations because of the finite thickness of the slabs. The shifts, however, are very small (in this work always less than 0.13 eV).

The projected DOS of the four important frontier orbitals, magnified by a factor of five, is displayed in Fig. 2. The horizontal 'sticks' display the positions of the MOs in a free, planar, undistorted ethene molecule. After adsorption, *ca.* 18% of the DOS of π is pushed up above the Fermi energy and the main body of this band is pushed down by *ca.* 0.5 eV. From the integration curve, *ca.* 44% of the π^* becomes occupied. It also develops substantial dispersion, indicative of strong interaction.

[†] 1 eV $\approx 1.602 \times 10^{-19}$ J.

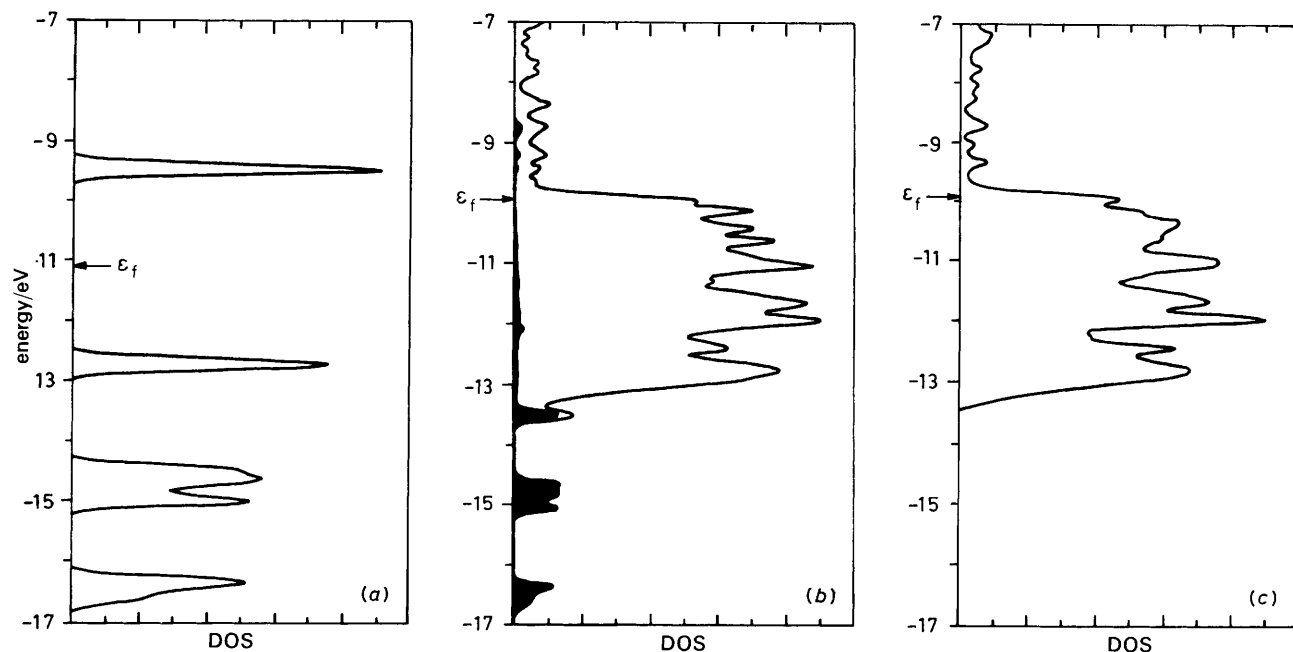


Fig. 1 (a) Total DOS of a monolayer of ethene arranged in the same geometry as the adsorbed layer at Ni(2-fold). (b) Total DOS of ethene (shaded) at Ni(2-fold) at one-quarter coverage. (c) Total DOS of Ni(111) surface

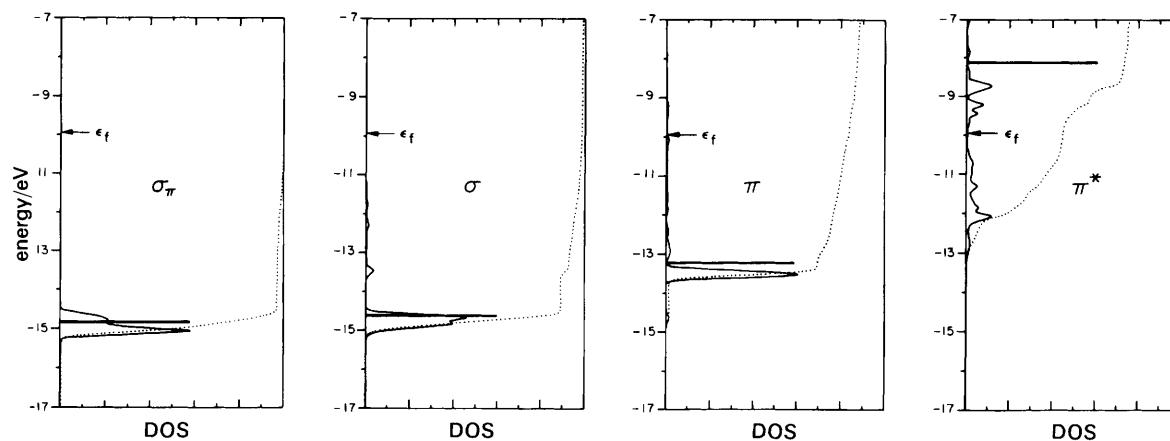


Fig. 2 Projected DOS of the four frontier orbitals of ethene at Ni(2-fold). The solid line and the dotted line are the DOS and integration curve, respectively

Let us examine the bonding in these chemisorbed ethenes by looking at the crystal orbital overlap population (COOP) curves in Fig. 3. In the left panel (a) are the COOP curves for the C–Ni bond. There are three important bonding regions defined in (a). Regions I and II consist of the bands near -14.5 eV and the sharp peak near -13.5 eV, respectively. Region III starts from the top of region II and goes up to the Fermi energy. Over 90% of the DOS of σ and σ_π can be found in the first region, while the π band is the major component of region II. A substantial amount of the DOS of π (ca. 10%), and nearly all the DOS of π^* that is below the Fermi energy, are located in region III. The bonding in region II is almost entirely due to π -to-metal forward donation, while in region III it is mainly the result of metal-to- π^* back-bonding and partly that of forward donation involving π .

A similar distribution of the DOS of the four frontier orbitals among the three bonding regions occurs at the on-top site of Ni(111) and the other two metal surfaces, Pd(111) and Pt(111). There are, however, two major trends. The DOS of π^* in region III decreases from the 2-fold site to

the on-top site. For a given adsorption site, it increases in the following order: Pd(111) \rightarrow Pt(111) \rightarrow Ni(111).

We can partition the contributions to adsorbate–surface bonding by energy region; this and other bonding information is listed in Table 5. From the electron population of π and π^* , the strongest forward donation and back-bonding seem to occur at the 2-fold site of Ni(111) and Pt(111), respectively.

The change in dispersion and electron occupation of σ and σ_π is not dramatic. Does this mean that σ and σ_π do not participate significantly in bonding to the surface? Although σ and σ_π show little change in electron occupation and do not develop substantial dispersion, they do interact with the surface, especially at the on-top site. For example, region I accounts for ca. 17% of the C–Pd OP at Pd(2-fold) but 44% at Pd(on-top). The COOP curves of Pt(on-top) in Fig. 3 show that the bonding peak in region I is actually larger than that in region II.

Our next goal is to determine whether σ or σ_π is the major source of ethene–metal bonding in this region. From its shape, σ should overlap much better with the metal orbitals

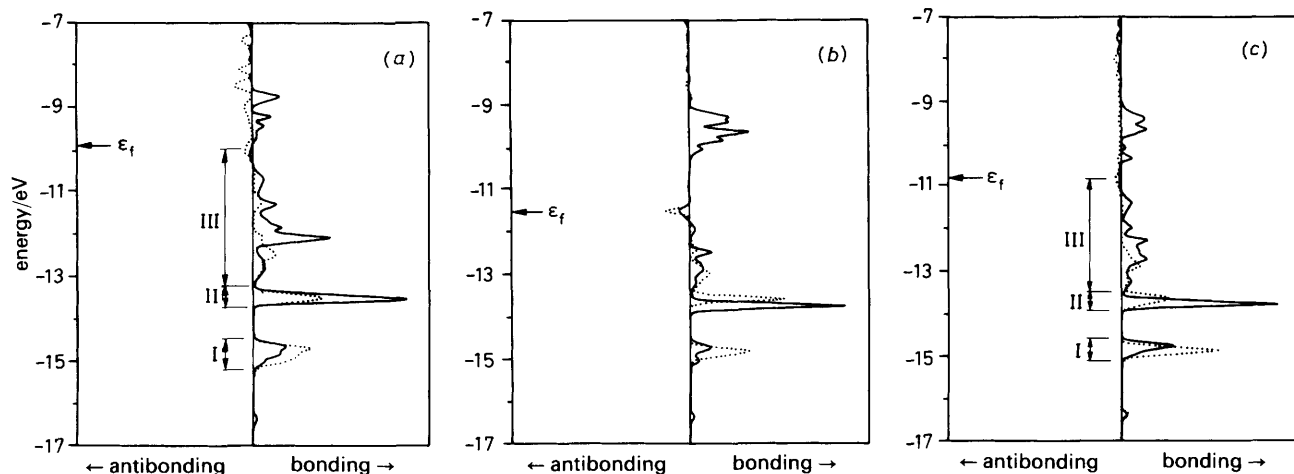
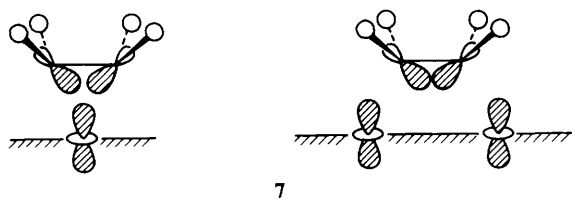


Fig. 3 (a) COOP curve for C—Ni bond. (b) COOP curve for C—Pd bond. (c) COOP curve for C—Pt bond. (···) On-top site; (—) 2-fold site

Table 5 Selected bonding information at the 2-fold site and the on-top site

| | 2-fold site | | | on-top site | | |
|--|-------------|---------|---------|-------------|---------|---------|
| | Ni(111) | Pd(111) | Pt(111) | Ni(111) | Pd(111) | Pt(111) |
| net charge on chemisorbed ethene | -0.55 | +0.03 | -0.19 | -0.31 | +0.06 | -0.04 |
| electron occupation of π^* | 0.89 | 0.32 | 0.69 | 0.60 | 0.24 | 0.43 |
| electron occupation of π | 1.68 | 1.65 | 1.54 | 1.74 | 1.71 | 1.66 |
| electron occupation of σ | 1.98 | 1.99 | 1.97 | 1.950 | 1.96 | 1.93 |
| electron occupation of σ_π | 1.99 | 1.99 | 1.99 | 1.99 | 1.99 | 1.99 |
| total carbon-metal overlap population (OP) | 0.371 | 0.212 | 0.394 | 0.229 | 0.165 | 0.271 |
| carbon-metal OP from region III | 0.159 | 0.044 | 0.141 | 0.064 | 0.036 | 0.070 |
| carbon-metal OP from region II | 0.130 | 0.123 | 0.139 | 0.069 | 0.076 | 0.074 |
| carbon-metal OP from region I | 0.055 | 0.035 | 0.068 | 0.096 | 0.072 | 0.114 |
| Fermi level/eV | -9.93 | -11.53 | -10.86 | -9.91 | -11.53 | -10.86 |

at the on-top site, as shown in 7. The reverse should be true for σ_π , because at the on-top site it is locally orthogonal to all orbitals of the nearest metal atoms. From the OP in Table 5 and the COOP curves in fig. 3, it can be seen that the ethene-metal interaction in region I decreases on going from the on-top to the 2-fold site, suggesting the dominance of σ over σ_π . This was confirmed by a numerical experiment, in which selected atomic overlaps between the surface and the adsorbate (those involved in σ_π) were dropped.



Since σ is quite important at the on-top site of Pd(111) (in region I, it accounts for 42% of the total C—Pd OP), it is worthwhile to identify the metal orbital that interacts strongly with it. Considering its orientation, a good candidate is d_{z^2} (s and p_z are eliminated because they would lead to substantial depopulation of σ). As shown in Fig. 4, region I picks up *ca.* 8% of the DOS of the nearest surface d_{z^2} orbital at Pd(on-top). Even in the absence of the adsorbate, the s , p_z and d_{z^2} of the surface atoms have the same symmetry and extensive hybridization is possible. It is therefore not a good idea to estimate the OP due to d_{z^2} by dropping the overlap. Instead we project out its contribution. In this way, mixing of orbitals induces no error. The projected OP for d_{z^2} in region I is 0.043. The total projected OP for all other metal orbitals is 0.030. The interaction of σ with the d_{z^2} in this region is thus significantly greater than that of the total of the other eight metal orbitals.

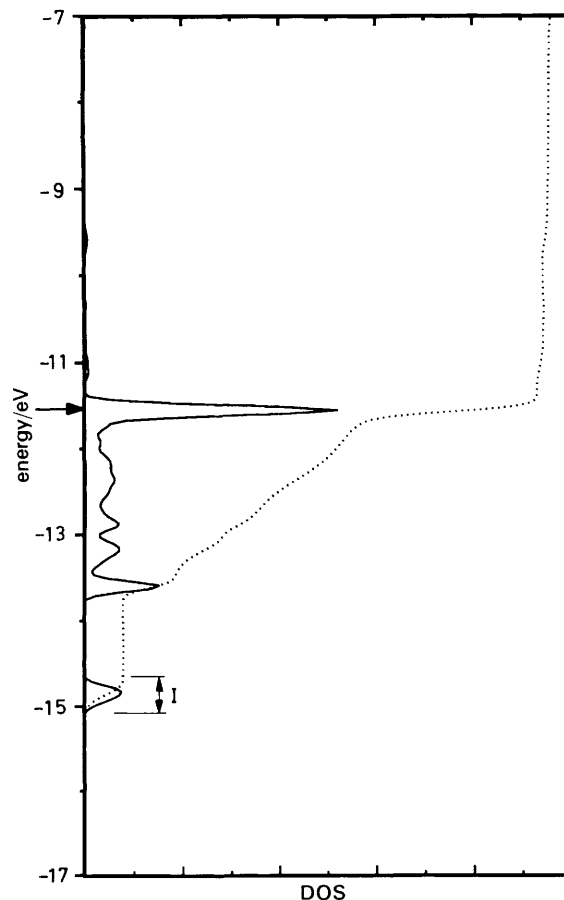


Fig. 4 Projected DOS (—) and integration curve (···) for the d_{z^2} orbital of Pd₁

π and π^* are the most active participants in the adsorbate-surface interaction in regions II and III. They undergo significant depopulation and population, respectively, upon adsorption. Their electron occupations also determine the net charge on the adsorbate, which is roughly equal to two minus their total electron population (see Table 5). On Ni(111) and Pt(111), the metal-to- π^* back donation of electrons outweighs the forward donation from π and the adsorbed ethene is negatively charged. The opposite occurs on Pd(111). As mentioned before, this may be due to its lower d bands. Notice that the σ band is always below the d block. A lower H_{ii} for the d orbitals means a better energy match for interaction. The percentage contribution of σ in region I to the metal-carbon OP is indeed greatest at the on-top site of Pd(111).

Detailed analysis of regions II and III, however, is not so simple because it involves contributions from σ , π and π^* , some bonding and some antibonding. The analytical tools we have used so far may not give us a sufficiently detailed picture of adsorbate-surface interaction. What we need is a method to project out the individual contribution from each FMO of ethene to the carbon-metal OP. In Table 6, the result of the partitioning of the total carbon-metal overlap populations by this method is presented.

Table 6 reveals several bonding features. First, we recall that there is strong interaction between the ethene σ orbital and the metal surfaces at the on-top site. σ -metal OPs, however, are not significant. In interpreting this apparent paradox, the σ -Pd COOP curve of Pd(on-top) in Fig. 5 is instructive. The bonding peak in region I is essentially neu-

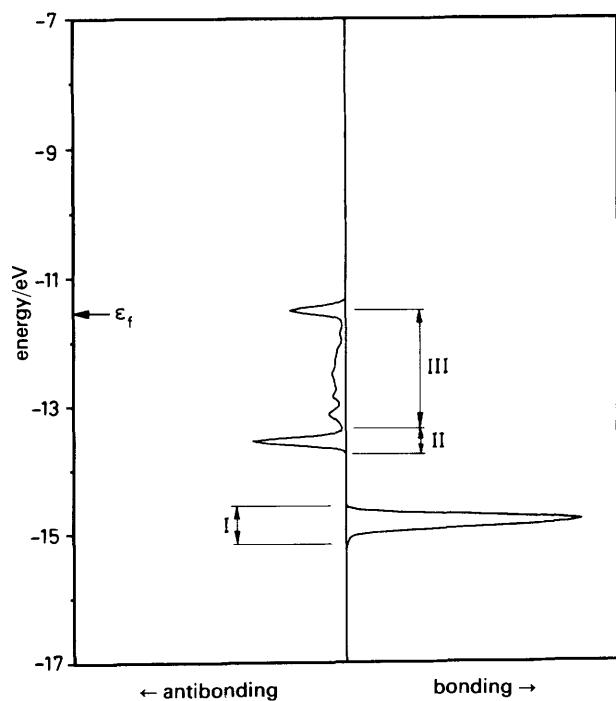


Fig. 5 σ -Pd₁ COOP curve

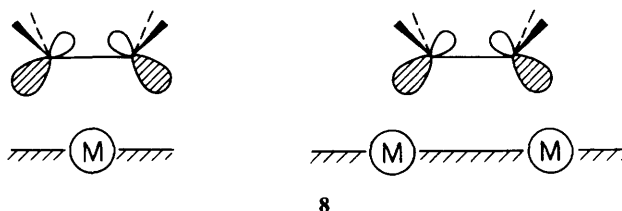
Table 6 Contributions of the four FMOs of ethene to the carbon-metal overlap populations

| FMO | 2-fold site | | | on-top site | | |
|---------------------------------------|-------------|---------|---------|-------------|---------|---------|
| | Ni(111) | Pd(111) | Pt(111) | Ni(111) | Pd(111) | Pt(111) |
| π^* | 0.236 | 0.108 | 0.215 | 0.118 | 0.072 | 0.113 |
| π | 0.137 | 0.119 | 0.172 | 0.108 | 0.118 | 0.140 |
| σ | -0.001 | -0.003 | 0.001 | 0.032 | 0.018 | 0.043 |
| σ_π | -0.005 | -0.002 | -0.003 | -0.002 | -0.001 | -0.002 |
| total metal-carbon overlap population | 0.371 | 0.212 | 0.394 | 0.229 | 0.165 | 0.271 |

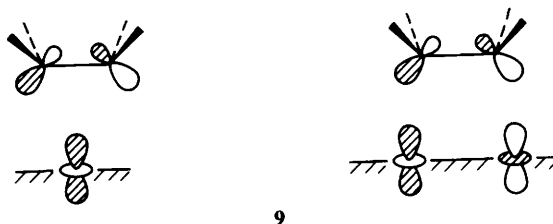
The contributions of the other eight FMOs are negligible.

tralized by antibonding interactions in regions II and III. Although there are good overlaps between σ and the d orbitals, the net effect is almost non-bonding. The fact that there is a substantial amount of the DOS of d_{z^2} in resonance with that of σ means there is strong interaction but not necessarily strong bonding. To have strong bonding, the antibonding counterpart has to be above the Fermi energy. This is exactly what happens when π and π^* interact with the metal. An analysis of bonding that is based solely on the DOS thus may be insufficient.

On Ni(111), probably because of the higher Fermi energy, π^* always contributes more to the metal-carbon overlap population than does π . The opposite occurs on Pd(111). For Pt(111), a transition can be observed: at the on-top site, π is more important, but at the 2-fold site, π^* is the major source of C-Pt bonding. According to the electron populations in Table 5, the COOP curves in Fig. 3 and the projected OP, the interaction of π and π^* with the metal surface strengthens on going from the on-top site to the 2-fold site. This may be due to a combination of two factors: *i.e.* orientation and symmetry. The lobes of π and π^* are pointing towards the metal atoms at the 2-fold site but away from them at the on-top site, 8.



For a π -bonded ethene, symmetry prevents any good overlap between π and the nearest metal p_x and d_{xz} . It also prohibits any effective interaction of π^* with the surface s , p_z and d_{z^2} , 9. There is another interesting but more subtle feature concerning π^* . For Ni(111) and Pt(111), the π^* -Ni₁ and π^* -Pt₁ OP decrease significantly (50% for the former and 46% for the latter), on changing from di- σ -bonded ethene to π -bonded adsorbate. The corresponding reduction of OP on Pd(111) is much smaller, only *ca.* 8%. In addition, if we compare the electron occupation of π^* between the two adsorption sites among the three metal surfaces, again there is a much smaller difference on Pd(111).



This differential weakening of π^* -metal interaction may be understood by examining Fig. 6. In the left panel (a) are the COOP curves for π^* -Pd₁ at Pd(2-fold) and Pd(on-top). By

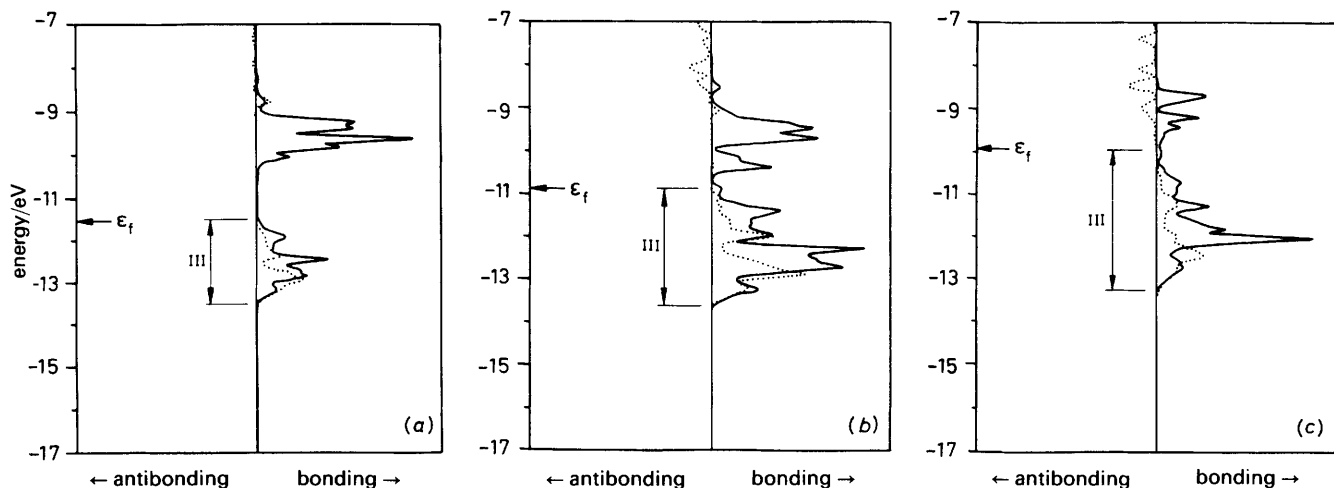
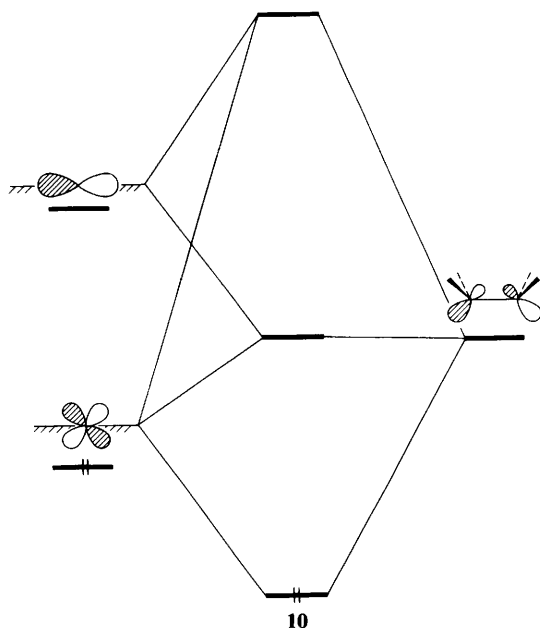


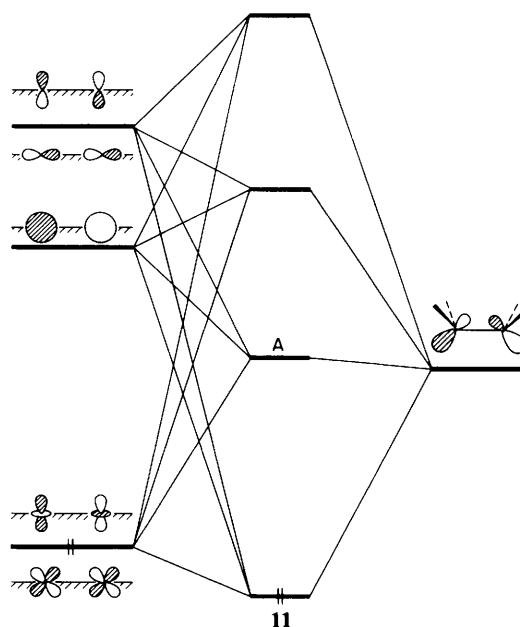
Fig. 6 (a) π^* -Pd COOP curve. (b) π^* -Pt COOP curve. (c) π^* -Ni COOP curve. (···) On-top site; (—) 2-fold site

projecting out the OP between π^* and individual palladium orbitals, it is found that the two bonding peaks at -12.5 eV (within region III) are mainly the result of interaction between π^* and d_{xz} at the on-top site, and π^* , d_{z^2} and d_{xz} at the 2-fold site. These two peaks are of similar size and hence the similar π^* -Pd₁ OP at Pd(2-fold) and Pd(on-top). Near -9.5 eV, where most of the DOS of π^* is located, the situation is completely different. For Pd(on-top), there is some π^* - p_x bonding interaction which is almost exactly cancelled out by the antibonding interaction between π^* and d_{xz} . The net result is that the orbitals in this region are mainly π^* -Pd non-bonding. For Pt(2-fold), the bands near -9.5 eV are π^* - d_{xz} and π^* - d_{z^2} antibonding but π^* - s , π^* - p_z and π^* - p_x bonding. The bonding interactions of s and p outweigh the antibonding interactions of d and a prominent bonding peak appears. (This peak actually is larger than that in region III.)

In summary, the π^* -Pd bonding at the on-top site may be represented schematically by a 'three-level' interaction diagram, 10. A characteristic outcome of this type of inter-



action is a non-bonding level in the middle. In this case, it corresponds to the π^* orbitals just above the Fermi energy. At the 2-fold site, if we consider p_x and p_z as one level, and d_{xz} and d_{z^2} as another, a 'four-level' interaction diagram of the type shown in 11 may be appropriate to describe the



π^* -Pd bonding. The second level, which is labelled as A, is the cause of the large bonding peak near -9.5 eV. The orbitals on the left-hand side of this drawing are meant to remind the reader that π^* can overlap effectively only with those metal orbitals that are Pd₁-Pd₂ antibonding.

The π^* -Pt₁ COOP curves are displayed in the middle panel (b) of Fig. 6. Part of A has been pushed down below the Fermi energy and the bonding peak near -9.5 eV is smaller than that in region III. The result is dramatic. In Pd(2-fold), the s and p bands account only for 27% of the π^* -Pd OP but in Pt(2-fold), their contribution to the π^* -Pt OP is *ca.* 50%. The π^* -surface bonding in the upper part of region III is dominated by the s and p bands. For Ni (111), as indicated by the COOP curves in the right panel (c), an even larger portion of A has penetrated into region III. Now over 59% of the π^* -Ni OP can be attributed to the s and the p orbitals. These results also fit the general trend that the chemistry of palladium is more similar to that of platinum than nickel.²⁶

Thus, it is the position of A relative to the Fermi energy that is mainly responsible for the differential reduction in the OP between π^* and the nearest surface atom on going from the 2-fold to the on-top site. The inability of the s and p orbitals of the palladium to push A down below the Fermi energy greatly diminishes the back-bonding, and Pd(2-fold) is

Table 7 Overlap population between π and the nine metal surface orbitals

| metal orbital | 2-fold site | | | on-top site | | |
|--|-------------|---------|---------|-------------|---------|---------|
| | Ni(111) | Pd(111) | Pt(111) | Ni(111) | Pd(111) | Pt(111) |
| s | 0.075 | 0.082 | 0.082 | 0.067 | 0.085 | 0.077 |
| p _x | 0.001 | 0.002 | 0.003 | 0 | 0 | 0 |
| p _z | 0.042 | 0.031 | 0.050 | 0.0290 | 0.027 | 0.039 |
| d _{x²-y²} | 0 | 0 | 0 | -0.001 | -0.001 | -0.001 |
| d _{z²} | 0.016 | 0.004 | 0.028 | 0.013 | 0.006 | 0.025 |
| d _{xz} | 0.003 | 0.001 | 0.009 | 0 | 0 | 0 |

The p_y, d_{xy} and d_{yz} interactions vanish by local symmetry, and are not listed.

Table 8 Overlap population between π^* and the nine metal surface orbitals

| metal orbital | 2-fold site | | | on-top site | | |
|--|-------------|---------|---------|-------------|---------|---------|
| | Ni(111) | Pd(111) | Pt(111) | Ni(111) | Pd(111) | Pt(111) |
| s | 0.078 | 0.017 | 0.061 | 0 | 0 | 0 |
| p _x | 0.003 | 0.003 | 0.004 | 0.018 | 0.005 | 0.017 |
| p _z | 0.058 | 0.009 | 0.043 | 0 | 0 | 0 |
| d _{x²-y²} | -0.001 | -0.001 | -0.001 | 0 | 0 | 0 |
| d _{z²} | 0.087 | 0.059 | 0.084 | -0.001 | 0 | 0 |
| d _{xz} | 0.010 | 0.020 | 0.023 | 0.100 | 0.067 | 0.097 |

The p_y, d_{xy} and d_{yz} interactions vanish by local symmetry, and are not listed.

the only 2-fold site at which π contributes more to the carbon-metal OP than π^* .

A more thorough, quantitative description of the bonding of π and π^* with the metal orbitals is given in Tables 7 and 8. Owing to a symmetry constraint, almost half of the OPs in these two tables are equal or close to zero. The OPs in Table 7 clearly show that the π -surface bonding occurs mainly *via* the metal s and p bands, in agreement with the concept of forward donation. Similarly, the idea of back-bonding is well illustrated by the results in Table 8.

So far, we have concentrated on the adsorbate. We now turn our attention to the surfaces. Generally, the greater the number of surface atoms directly bonded to the adsorbate, the greater will be the bond weakening within the surface. The metal-metal OPs, however, indicate that the degree of bond weakening at the surface for both the on-top and 2-fold sites is essentially the same, that is, this factor is not crucial in determining the site preference. One would like to separate the carbon-metal OP into nine components, corresponding to the contribution of each orbital of the metal atoms involved in anchoring the ethene. The s and p bands of a transition metal are very diffuse. Their band widths are tens of eV. The changes in the DOS of these orbitals after adsorption are thus much less obvious than those of the d bands. As a result, the role of the s and p orbitals on chemisorption involving transition metals is seldom discussed, although, by analogy to organometallic compounds, these orbitals should

interact with the adsorbate. The role of their counterparts, the more contracted d orbitals, may be over-emphasized in the existing literature discussions, including our own. The partitioning of the carbon-metal OP (Table 9) may provide more insight on this issue.

There is little doubt that the d orbitals are involved in adsorbate-surface bonding, but the combined effect of the s and p bands is much more important. In fact, apart from the on-top site on Ni(111), the s orbital alone contributes more to the carbon-metal OP than all of the five d orbitals do together. As shown by the OP in Tables 7 and 8, the reason behind this is that, apart from forward donation, the surface s and p bands participate actively in π^* -metal bonding. In all adsorption sites, p_y, d_{xy} and d_{yz} are orthogonal to σ , π and π^* . Most of the interaction between p_x and metal surfaces occurs above the Fermi energy. d_{x²-y²} may engage heavily in metal-metal bonding. Hence these five orbitals play only a minor role in surface-adsorbate bonding.

The interaction between ethene and the surface s, p_z and d_{z²} bands reduces substantially as one moves from the 2-fold to the on-top site. From the previous discussion, we think that this may be related to the symmetry of π^* . To confirm our conjecture, we take a close look at the COOP curves between Ni s and carbon in Fig. 7. For the 2-fold site, there is a significant bonding contribution from region III, indicative of a strong interaction with the π^* orbital. π^* is orthogonal to the nearest surface s orbital at the on-top site. Effective

Table 9 Contribution of the nine metal orbitals to the carbon-metal overlap populations

| metal orbital | 2-fold site | | | on-top site | | |
|--|-------------|---------|---------|-------------|---------|---------|
| | Ni(111) | Pd(111) | Pt(111) | Ni(111) | Pd(111) | Pt(111) |
| s | 0.169 | 0.117 | 0.160 | 0.095 | 0.105 | 0.105 |
| p _x | 0.004 | 0.005 | 0.010 | 0.019 | 0.007 | 0.019 |
| p _y | -0.001 | -0.000 | -0.001 | -0.002 | -0.003 | -0.001 |
| p _z | 0.092 | 0.015 | 0.089 | 0.022 | -0.000 | 0.036 |
| d _{x²-y²} | -0.002 | -0.002 | -0.002 | -0.001 | -0.001 | -0.001 |
| d _{z²} | 0.104 | 0.062 | 0.110 | -0.003 | -0.001 | 0.018 |
| d _{xy} | 0.001 | -0.000 | 0.000 | -0.001 | -0.0010 | -0.001 |
| d _{xz} | 0.010 | 0.020 | 0.031 | 0.101 | 0.067 | 0.097 |
| d _{yz} | -0.005 | -0.005 | -0.005 | -0.000 | -0.001 | -0.001 |

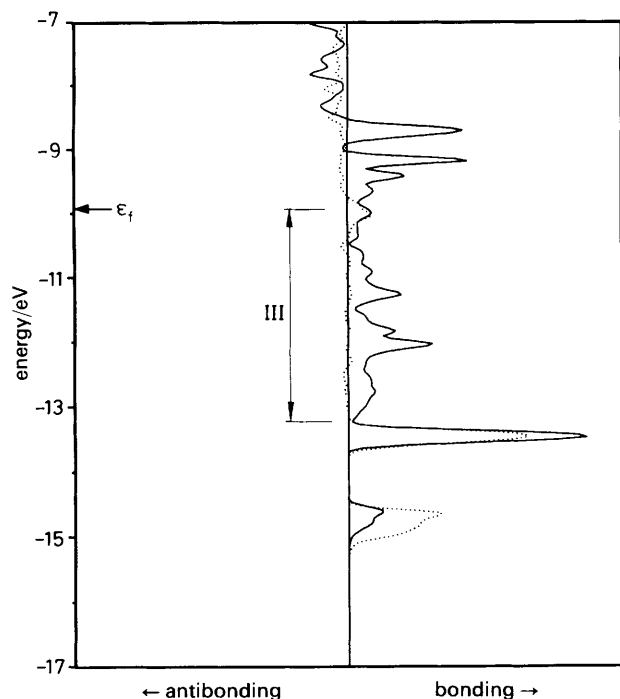
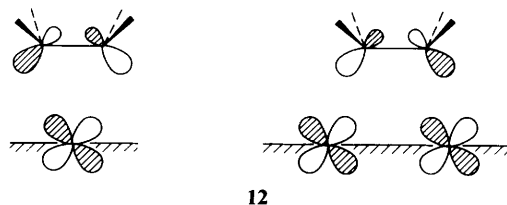


Fig. 7 Contribution of the nickel s orbital to the Ni-C COOP curve. (···) On-top site; (—) 2-fold site

overlap is thus prohibited and the bonding interaction is much smaller. A similar argument seems to apply to the p_z and d_{zz} orbitals.

In contrast to other metal orbitals, the projected OP of d_{zz} is much larger at the on-top site. To trace the reason for this, we examine the COOP curves for the carbon atom and the Ni d_{zz} in the left panel of Fig. 8. At the on-top site, d_{zz} is orthogonal to the σ , σ_π and π orbitals of ethene. The interactions in the first two regions are thus negligible. For the 2-fold site, the symmetry constraint is partially relaxed. σ , π and the part of the surface d_{zz} band that is Ni_1 - Ni_2 bonding

undergo a 'three-level' interaction. However, the greatest difference occurs in region III. In Ni(2-fold), π^* can overlap effectively only with the upper part of the surface d_{zz} band that is Ni_1 - Ni_2 antibonding. In Ni(on-top), it can interact extensively with the whole d_{zz} band, as shown in 12. Thus a



much larger C- d_{zz} OP results (see Table 8). The COOP curve in the right panel is meant to illustrate the characteristics of the above 'three-level' interaction; the lowest level is strongly bonding, the middle level essentially non-bonding and the third level is strongly antibonding.

It is instructive to examine the partitioning of the Ni-C COOP curves into the s, p and d components. As expected, in Fig. 9 the s and p bands produce large bonding peaks in region II, where most of the DOS of π can be found, corresponding the π -to-metal forward donation. Surprisingly, this is also true for the d orbitals. This would induce some antibonding interaction within region III. Hence the unexpectedly small contribution of the d bands to the carbon-metal OP (relative to s and p) is due to the antibonding peaks in region III, as a direct result of interactions of the d bands with filled orbitals of ethene. (We see here a surface analogue of the molecular two-level four-electron repulsion.³) The partitioning of the C-Pd and C-Pt COOP curves shows similar features.

The Organometallic Analogy

It is instructive to compare the computational results for the three on-top sites with those of discrete, molecular η^2 coordinated (π -bonded) olefinic complexes, studied in a previous paper.³⁵ Unfortunately ethenes were kept planar in the molec-

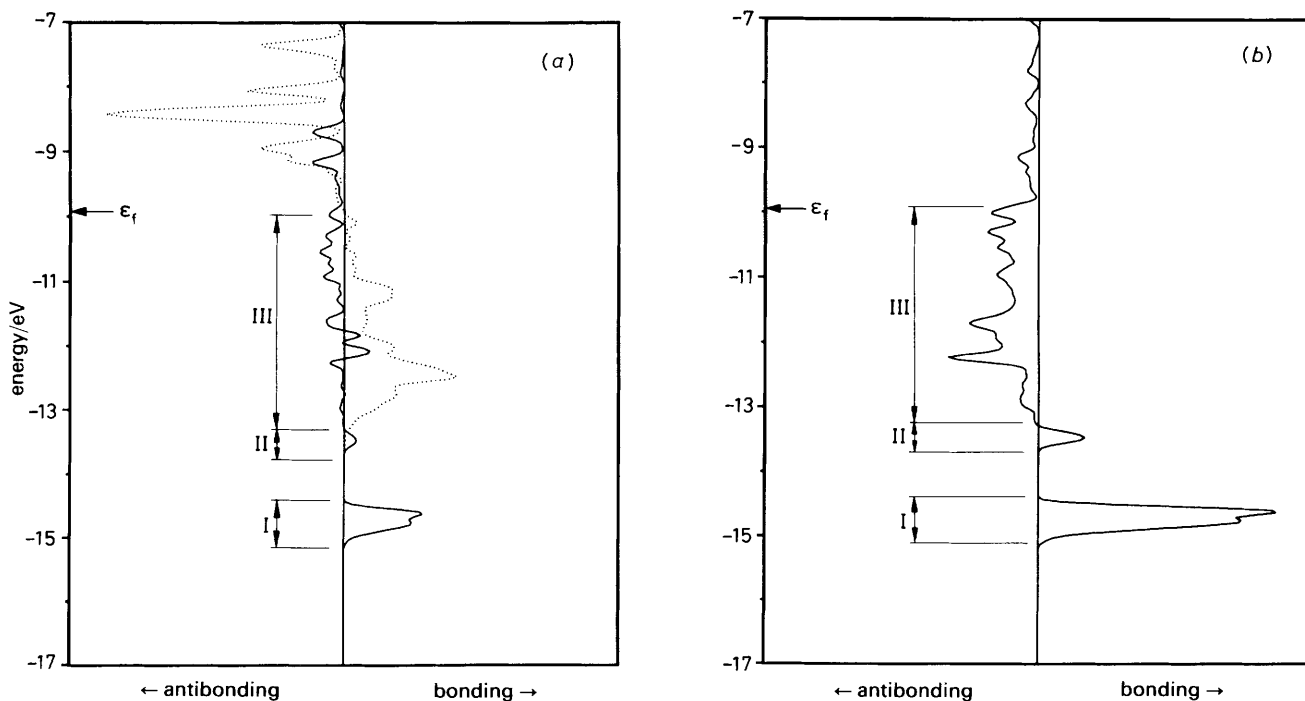


Fig. 8 (a) COOP curve for the d_{zz} orbital of surface nickel atoms and ethene. (b) COOP curve for the interaction of the σ and π orbital of ethene with the d_{zz} orbitals of the surface nickel atoms. (···) On-top site; (—) 2-fold site

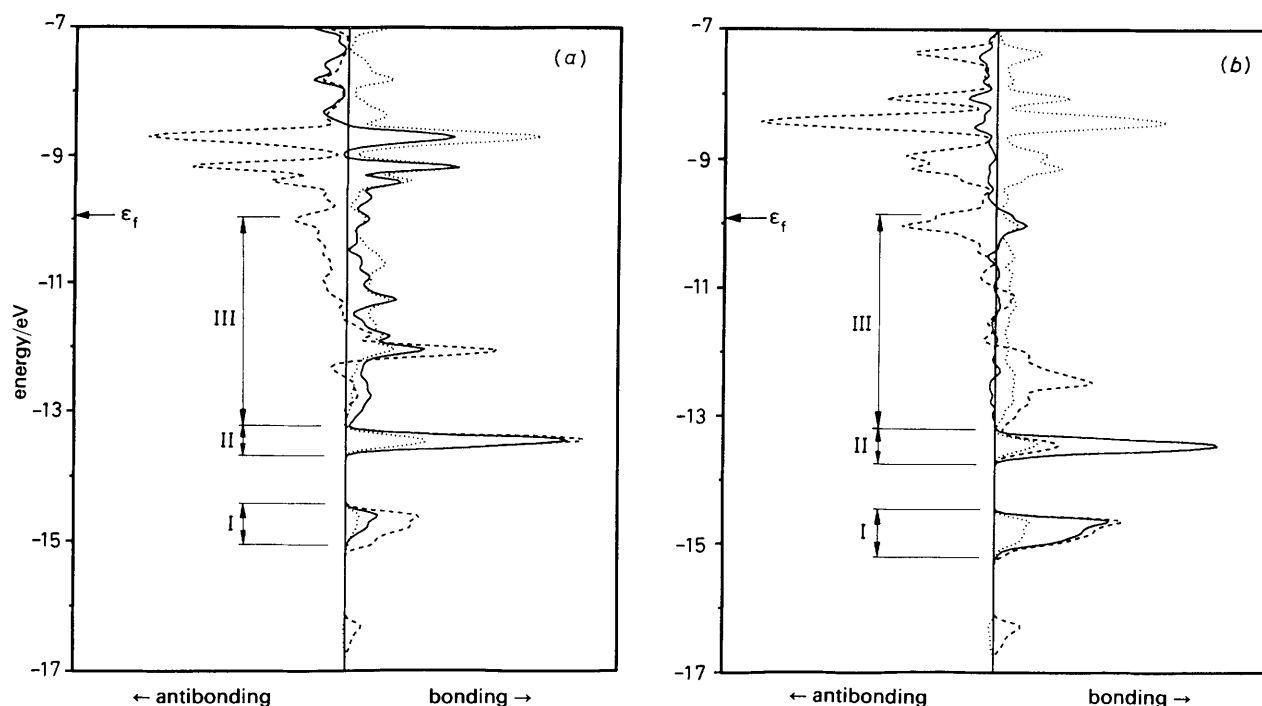
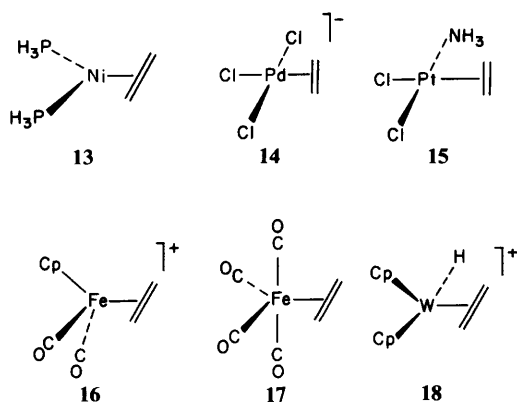


Fig. 9 Partition of the C-Ni COOP curve for (a) Ni(2-fold) and (b) Ni(on-top). (---) d component; (···) p component, (—) s component

ular calculations, for reasons of simplicity. For comparison, we planarize our adsorbates and repeat the calculations. Selected information is collected in Table 10, where the occupation of the π and π^* orbitals of ethene for molecules 13–18 is reported. Note the generally similar occupations for discrete molecules and surfaces for a given metal and the wider range of occupations in known organometallic olefin complexes.



There are certainly many similarities between the organometallic compounds and surface complexes. Yet there are differences too. For instance, the energy of the HOMO depends strongly on the nature of the ligand, while the metal

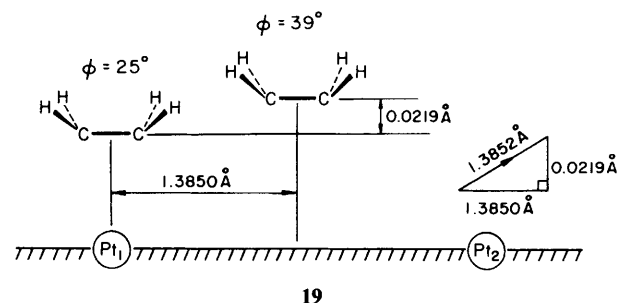
Table 10 Electron density of π and π^* and the net charge on ethene

| system | π | π^* | net charge |
|---|-------|---------|------------|
| Ni(PH ₃) ₂ C ₂ H ₄ | 1.81 | 0.44 | -0.28 |
| Ni(on-top) | 1.76 | 0.47 | -0.27 |
| (PdCl ₃ C ₂ H ₄) ⁻ | 1.71 | 0.21 | +0.02 |
| Pd(on-top) | 1.66 | 0.35 | +0.01 |
| cis-PtCl ₂ NH ₃ C ₂ H ₄ | 1.64 | 0.24 | +0.10 |
| Pt(on-top) | 1.66 | 0.35 | +0.01 |
| CpFe(CO) ₂ C ₂ H ₄ ⁺ | 1.53 | 0.32 | +0.20 |
| Fe(CO) ₄ C ₂ H ₄ | 1.66 | 0.48 | -0.15 |
| Cp ₂ WHC ₂ H ₄ ⁺ | 1.74 | 0.60 | -0.36 |

Fermi energy is not affected by the adsorbate molecules. The work function of the metal does vary after chemisorption, owing to a change in the surface dipole.

Interconversion of π -bonded and Di- σ -bonded Ethene

To our knowledge, there have been two reports on the transformation of π -bonded ethene to a di- σ -bonded adsorbate on Pt(111).^{17,36} We would like to estimate the activation energy of this process. Given our geometries, the transformation involves a translational motion of 1.3852 Å and an increase in the bending angle of the HCH plane (ϕ , see 3) of 14°. We thus assume a reaction pathway in which there is an increase of 1.4° in the bending angle for every linear translation of 0.13852 Å, 19. In Fig. 10, we present the potential-energy



curve for this transformation. The activation energy was found to be 0.22 eV. Hence the transformation seems to be energetically feasible, this is a small energy. By assuming a similar reaction pathway (one degree decrease in bending angle, ϕ , per linear translation of 1.3752 Å), the activation energy for the conversion of the 2-fold site on Pd(111) to the on-top site was estimated to be 0.14 eV.

There have been some indications of the existence of π -bonded ethene on Pt(111).^{12,17,36} Since the energy differences for the two adsorption sites on the two surfaces, Pd(111) and Pt(111), are similar (but opposite in order) and the activation energies for transformation are roughly the same, it may be worthwhile to try to detect the di- σ -bonded species on

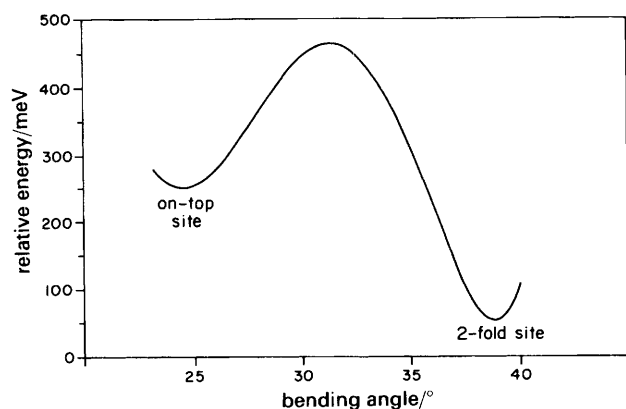


Fig. 10 Energy profile for the interconversion of ethene between Pt(2-fold) and Pt(on-top)

Pd(111). However, the energy barrier for the transformation of ethene from the on-top site on Ni(111) to the 2-fold site was calculated to be 0.0026 eV. The π -bonded species on Ni(111) seems to be thermodynamically and kinetically unstable with respect to the di- σ -bonded ethene, and its detection may be more difficult.

Conclusions

We have investigated in detail the adsorption of ethene on three metal surfaces, Ni(111), Pd(111) and Pt(111). Several established and useful concepts in molecular chemistry, such as the Dewar–Chatt–Duncanson model, local symmetry and three level interactions, are valuable for understanding the adsorbate–surface interaction. There are, however, some unexpected results as well. It seems that besides the d bands, the s and p bands also play a significant role in the bonding between π^* and the surface. Although the σ orbital of ethene interacts strongly with the metal atoms, the contribution of this orbital to bonding is not significant because most of the σ -surface antibonding states are below the Fermi energy. In contrast, most of the π -surface and π^* -surface bonding states are occupied while their antibonding counterparts are empty. Hence, these two frontier orbitals dominate the adsorbate–surface bonding. π^* is the major contributor to the carbon–metal OP for Ni(2-fold), Ni(on-top) and Pt(2-fold), but π is more important for the other three adsorption sites. On Ni(111) and Pt(111), the π^* -metal bonding is much stronger at the 2-fold site than the on-top site, mainly due to level A (see scheme 11). This may be related to the slight energetic preference for Ni(2-fold) and Pt(2-fold) relative to Ni(on-top) and Pt(on-top), although at the 2-fold site there is more weakening of the C–C bond. For Pd(2-fold), most of the π^* -s and π^* -p bonding states are above the Fermi energy. As reflected by the electron occupation and the projected OP, the π^* -Pd interaction is only slightly strengthened on going from Pd(on-top) to Pd(2-fold). This small gain in bonding energy may not be enough to compensate for the C–C weakening, and thus Pd(on-top) is the more stable site.

Appendix

Our calculations are of the tight-binding extended Hückel type with weighted H_{ij} approximations.^{37,38} The geometrical assumptions concerning bond lengths (in Å) include the following: C–H, 1.10; C–C, 1.45; Ni–C, 2.02; Pd–C, 2.10; Pt–C, 2.10; Ni–Ni, 2.49; Pd–Pd, 2.75; and Pt–Pt, 2.77 Å. The extended Hückel parameters are listed in Table 11. Double zeta expansions of the metal d orbitals have been employed. The parameters of ethene are taken from a pre-

Table 11 Extended Hückel parameters

| atom | orbital | H_{ii}/eV | ζ_1 | ζ_2 | c_1 | c_2 |
|------|---------|--------------------|-----------|-----------|-------|-------|
| C | 2s | -21.4 | 1.62 | | | |
| | 2p | -11.4 | 1.62 | | | |
| H | 1s | -13.6 | 1.30 | | | |
| | | | | | | |
| Ni | 4s | -7.92 | 2.10 | | | |
| | 4p | -4.18 | 2.10 | | | |
| | 3d | -11.51 | 5.75 | 2.00 | 0.57 | 0.63 |
| Pd | 5s | -7.51 | 2.19 | | | |
| | 5p | -3.86 | 2.15 | | | |
| | 4d | -12.53 | 5.98 | 2.61 | 0.55 | 0.67 |
| Pt | 6s | -8.82 | 2.55 | | | |
| | 6p | -5.28 | 2.55 | | | |
| | 5d | -12.15 | 6.01 | 2.70 | 0.63 | 0.55 |

vious study.³⁹ Charge iterations have been performed, assuming a quadratic dependence of metal H_{ii} s on charge.⁴⁰

The detailed procedure for obtaining the metal parameters is as follows: First we assume a bending angle of 30° for all six adsorption sites. We performed the charge iterations to get a set of H_{ii} s, calling them A. We then optimized the bending angles, ϕ , with set A. Repeating the charge iterations with these ϕ , we obtained another set of parameters, set B. Since set A was almost equal to set B, ϕ remained unchanged even if we repeated the optimization of bending angles with set B. The parameters used and listed in this paper are set B.

The k points are generated according to the geometrical method of Böhm and Ramirez.⁴¹ Since all of the six adsorption sites have the same symmetry, the same k point set (in total 18) can be and has been chosen for all calculations. In this way, the error in computing the energy difference between the on-top and 2-fold site should be minimized.

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