

Tuning of Metal–Metal Bonding by Counterion Size in Hypothetical AeTiO₂ Compounds

Xiao-Dong Wen, Thomas J. Cahill, Roald Hoffmann,* and Akira Miura

Department of Chemistry and Chemical Biology, Cornell University, Baker Laboratory, Ithaca, New York 14853-1301

Received July 31, 2009; E-mail: rh34@cornell.edu

No question that in predominantly ionic crystals cation or anion size may influence, greatly, unit cell dimensions and choice of structure type. We show here theoretical indications of significant cation-size tuning of a metal–metal bond in a partially ionic crystal.

We have been studying a *P4/mmm* ABX₂ structural type (Figure 1) suggested by M. J. Bucknum, who termed it “Kentuckia”.¹ Its already realized examples are CaCuO₂² and SrFeO₂.³ In the course of exploring variants of this structure, we came upon a hypothetical SrTiO₂ compound.

The undercoordinated Ti (and Sr) is obvious. What emerged from DFT calculations was a locally stable structure (confirmed by computation of phonon modes; details provided in the Supporting Information (SI) with an optimized lattice parameter *c* = 3.647 Å. That is also the Ti–Ti distance, and it is long, beyond what one would normally associate with a bond. But in the electronic structure of SrTiO₂ (formally Ti²⁺) a surprise awaited us—a pattern of bands characteristic of a one-dimensional metal along *c* and a Ti–Ti overlap population (OP, calculated with the extended Hückel (eH) method) of 0.29, despite that long Ti–Ti separation.

Thinking the Ti atoms along *c* “wanted” to be closer together, we decided to let them, by trying three smaller alkaline earth (Ae) cations (Be, Mg, and Ca). For good measure, we also tried a larger one (Ba). Given the formal d² configuration, one should consider the magnetism of these structures. Using a supercell, we computed antiferromagnetic (AFM) and ferromagnetic (FM) structures for all the phases: the structures emerged nonmagnetic for Ae = Be, Mg, Ca, and Sr. In the barium analogue, however, the FM BaTiO₂ (0.26 μ_B) is 0.06 eV per formula unit more stable than the AFM variant.

The results of structure optimization in the series are shown in Table 1. Not all of these compounds may be dynamically stable; in phonon calculations, the Be and Mg compounds show imaginary frequencies. On the other hand, AeTiO₂ with large counterions, Ae = Ca, Sr, or Ba, are all stable. There is a dramatic effect of the alkaline earth cation, Ae, on the *c* dimension in these compounds and a direct dependence on the cation size. For the smallest cations, the *c* axis length is in the range of typical Ti–Ti bonds; for the largest cations, it is very long. Yet there is still some Ti–Ti bonding at these long distances, as indicated by the overlap population (OP).

Where does the Ti–Ti bonding come from in this structure? The band structure of CaTiO₂ (Ti–Ti 3.332 Å) is shown in Figure 2. Notice the high dispersion band crossing the Fermi level (Γ→Z); it is largely made up of d_{z²} orbitals. Another band made up of d_{xz}+d_{yz} is partially occupied. The behavior of the levels along the Γ→Z direction is characteristic of a one-dimensional metallic chain: d_{z²} band going sharply up, d_{xz}+d_{yz} going down.^{4,5} This bonding pattern is present in all five Kentuckia phases studied.

Representative orbitals at the top and bottom of the d_{z²} and d_{xz}+d_{yz} bands are shown in Scheme 1. Since the bottom portions of each band are filled, we effectively have both σ and π bonding along *z*, an approach to a Ti=Ti double bond.

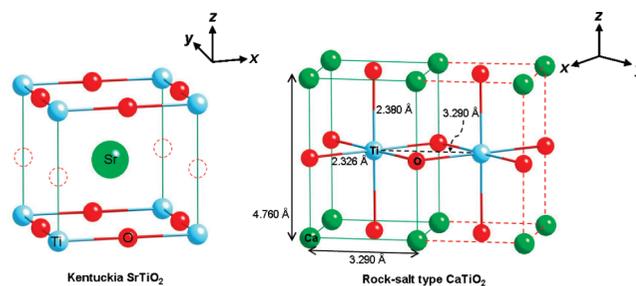


Figure 1. Left: The *P4/mmm* Kentuckia structure (ABX₂), atoms specified for SrTiO₂. The relationship to the perovskite structure is emphasized in this view; a true perovskite would also include the atoms indicated by the dotted red empty circles. Right: An ordered rock-salt type CaTiO₂ structure.

Table 1. Computed Lattice Constants (DFT) and the Ti–Ti Overlap Population Values (OP, eH) in Five Kentuckia AeTiO₂ Structures

	<i>a</i> (Å)	<i>c</i> (Å) = Ti–Ti	Ti–Ti OP
BeTiO ₂	3.911	2.856	0.36
MgTiO ₂	3.958	3.105	0.35
CaTiO ₂	3.993	3.332	0.34
SrTiO ₂	4.036	3.647	0.29
BaTiO ₂	4.075	4.129	0.23

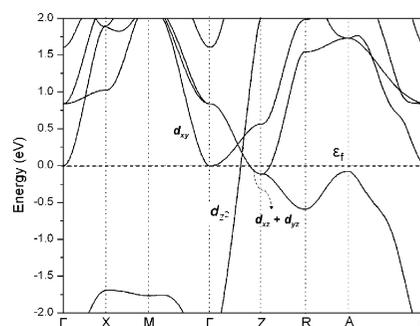
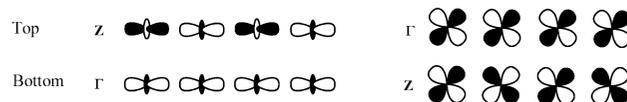


Figure 2. Band structure of nonmagnetic CaTiO₂ (DFT), in a small energy window around the Fermi level.

Scheme 1



Ti(II) compounds, extended or molecular, are rare. Apart from TiO (defect rock-salt, much nonstoichiometry in this structure)^{6,7} and the titanium halides TiX₂ (X = Cl, Br, I) which crystallize in the CdI₂ structure, there are very few other well-established Ti(II) extended structures.^{8–10}

Table 2. Computed Reaction Energy (ΔE) for Five Hypothetical Reactions^a

reaction	ΔE (eV)	CaTiO ₂	SrTiO ₂	BaTiO ₂
(1) AeTiO ₂ → Ae + TiO ₂		+1.57	+1.46	+1.25
(2) AeTiO ₂ → AeO + TiO		+0.20	+0.69	+0.98
(3) 3AeTiO ₂ → Ti ₂ O + 2AeO + AeTiO ₃		-0.08	+0.29	+0.81
(4) AeTiO ₂ + 1/2 O ₂ → AeO + TiO ₂		-4.69	-4.30	-4.07
(5) AeTiO ₂ + 1/2 O ₂ → AeTiO ₃		-4.96	-6.39	-5.31

^a We used optimized structures for fcc Ca and Sr, bcc Ba, rutile TiO₂, rock-salt AeO and TiO.

Are the AeTiO₂ structures we propose realistic? We investigated computationally the potential decomposition or combustion reaction energy (ΔE) of five pretty straightforward reactions shown in Table 2.

The first two simple alternative decomposition pathways, (1) and (2), are endothermic, which is encouraging. (3) is exothermic only for CaTiO₂. We also looked at two reactions, (4) and (5), involving O₂, the latter being the perovskite formation. These reactions were exothermic. Nothing surprising here, perovskites and Ti⁴⁺ compounds are common structures. Before the synthesis of SrFeO₂ from its parent perovskite SrFeO₃ in 2007,³ one might have viewed the great perovskite stability as an impediment to the existence of AeTiO₂ compounds. No longer; we think these compounds might be possible to make.

But one should think of other structural possibilities for AeTiO₂. Both TiO and CaO have a rock-salt structure, and Ca and Ti have similar ionic radii. So a rock-salt CaTiO₂ phase is a possibility.

We optimized the ordered rock-salt type CaTiO₂ structure shown in Figure 1 (right). This structural variant is 0.21 eV per CaTiO₂ more stable than Kentuckia (Figure 1, left) and is dynamically stable (no imaginary frequencies in phonon spectrum). The Ti–O distances are longer than a typical Ti–O bond: Ti–O bonds range from 1.92 to 1.98 Å in rutile, anatase and brookite TiO₂.^{11,12} The nearest four Ti distances are long 3.290 Å, but the computed Ti–Ti OP (eH) is 0.19, indicating net bonding in the *ab* plane. For calibration, the Ti–Ti bond length in rutile TiO₂ is shorter, 2.959 Å, but the rutile Ti–Ti OP is only 0.02.

The magnetism of rock-salt CaTiO₂ is quite different from that of the Kentuckia structure. The AFM rock-salt structure (using a $\sqrt{2} \times \sqrt{2} \times 2$ supercell) is preferred to the FM alternative by 0.06 eV per CaTiO₂; the calculated Ti magnetic moment is 1.3 μ_B .

The rock-salt structure is more stable than the Kentuckia geometry for Ae = Be (by -2.06 eV/BeTiO₂), Mg (-1.56 eV), and Ca (-0.21 eV) and less stable for Sr (+0.71 eV) and Ba (+1.94 eV). An analysis of the phonon modes for these structures is given in the SI.

What other structures might be reasonable? There is no dearth of alternatives. We began with what were perceived as related structures. A search of the Inorganic Crystal Structure Database (ICSD) revealed approximately a dozen AMX₂ (A = alkali metal or alkaline earth metal, X = O, S, Te, or N) structures with M = Ti, Zr, or Hf. None are formally M²⁺ but rather M³⁺⁴⁺. AeTiO₂ was studied in three of the structural types found: *R3m* (e.g., NaTiO₂), *P4/nmm* (e.g., SrTiN₂), *P3m1* (e.g., LiTiS₂), and *P6₃/mmc* (NaTiS₂). The calculated energies per formula unit were

significantly higher (>0.30 eV) for these structural alternatives, compared to the Kentuckia structure (see SI).

We moved next to evolutionary structure prediction, utilizing USPEX.^{13–15} A USPEX search for SrTiO₂ and BaTiO₂ leads to the Kentuckia structures. For CaTiO₂, the lowest energy structure (-0.40 eV per CaTiO₂ relative to Kentuckia) was of rock-salt type, but one different from the previous rock-salt structure. Going along an -M–O–M–O–M– chain, this structure was not strictly alternating -Ti–O–Ca–O–Ti–O–Ca– but a less symmetrical variant. Clearly there are going to be many “polymorphs” of the rock-salt structure; it is not easy to examine them all. Annealing molecular dynamics (MD) calculations undertaken on the Kentuckia AeTiO₂, Ae = Ca, Sr, or Ba, structures (2000–100 K) did not alter the phase.

To our knowledge, there are no AeTiO₂ phases known. The reaction of TiO₂ with Ae metals (Ae = Mg, Ca, Sr, and Ba) at 950 °C for 7 days gave AeO, AeTiO₃, Ae₂TiO₄, AeTi₄O₉, TiO, and Ti₂O phases but not the computed Kentuckia or rock-salt AeTiO₂ phases. The corresponding powder X-ray diffraction (pXRD) patterns (experimental and simulated) are shown in the SI. Perhaps a low-temperature synthetic method³ provides a better pathway to the preparation of AeTiO₂.

Rock-salt or Kentuckia in structure, this would be an interesting set of compounds.

Acknowledgment. Our work at Cornell was supported by the National Science Foundation through Grant CHE-0613306. This research was also supported in part by the National Science Foundation through TeraGrid resources provided by [NCSA].

Supporting Information Available: The computational methods summary, the band structures and DOS, the corresponding optimized structures with absolute energies, the experimental synthetic procedure, experimental and computational pXRD patterns, and phonon dispersion. This material is available free of charge via the Internet at <http://pubs.acs.org>.

References

- (1) Bucknum, M. J.; Castro, E. A. *Russ. J. Gen. Chem.* **2006**, *76*, 265.
- (2) Siegrist, T.; Zahurak, S. M.; Murphy, D. W.; Roth, R. S. *Nature* **1988**, *334*, 231.
- (3) Tsujimoto, Y.; Tassel, C.; Hayashi, N.; Watanabe, T.; Kageyama, H.; Yoshimura, K.; Takano, M.; Ceretti, M.; Ritter, C.; Paulus, W. *Nature* **2007**, *450*, 1062.
- (4) Hoffmann, R. *Solids and Surfaces: A Chemist's View of Bonding in Extended Structures*; WILEY-VCH: New York, 1988.
- (5) Burdett, J. K. *Chemical Bonding in Solids*; Oxford University Press: Oxford, UK, 1995.
- (6) Banus, M. D.; Reed, T. B.; Strauss, A. J. *Phys. Rev. E* **1972**, *5*, 2775.
- (7) Hughbanks, T.; Burdett, J. J. *Am. Chem. Soc.* **1984**, *106*, 3101.
- (8) Baenziger, N. C.; Rundle, R. E. *Acta Crystallogr.* **1948**, *1*, 274.
- (9) Greenwood, N. N.; Earnshaw, A. *Chemistry of the Elements*, 2nd ed.; Butterworths/Heinemann: Oxford, 1997; Chapter 22, pp 961–975.
- (10) Kölle, U.; Kölle, P. *Angew. Chem., Int. Ed.* **2003**, *42*, 4540.
- (11) Meagher, E. P.; Lager, G. A. *Can. Mineral.* **1979**, *17*, 77.
- (12) Horn, M.; Schwerdtfeger, C. F.; Meagher, E. P. *J. Am. Ceram. Soc.* **1970**, *53*, 124.
- (13) Glass, C. W.; Oganov, A. R.; Hansen, N. *Comput. Phys. Commun.* **2006**, *175*, 713.
- (14) Oganov, A. R.; Glass, C. W. *J. Chem. Phys.* **2006**, *124*, 244704.
- (15) Oganov, A. R.; Glass, C. W.; Ono, S. *Earth Planet Sci. Lett.* **2006**, *241*, 95.

JA9064766